Automatic alignment and reconstruction of images for soft X-ray tomography

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Soft X-ray tomography (SXT) is a powerful imaging technique that generates quantitative, 3D images of the structural organization of whole cells in a near-native state. SXT is also a high-throughput imaging technique. At the National Center for X-ray Tomography (NCXT), specimen preparation and image collection for tomographic reconstruction of a whole cell require only minutes. Aligning and reconstructing the data, however, take significantly longer. Here we describe a new component of the high throughput computational pipeline used for processing data at the NCXT. We have developed a new method for automatic alignment of projection images that does not require fiducial markers or manual interaction with the software. This method has been optimized for SXT data sets, which routinely involve full rotation of the specimen. This software gives users of the NCXT SXT instrument a new capability – virtually real-time initial 3D results during an imaging experiment, which can later be further refined. The new code, Automatic Reconstruction 3D (AREC3D), is also fast, reliable, and robust. The fundamental architecture of the code is also adaptable to high performance GPU processing, which enables significant improvements in speed and fidelity.

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1. Introduction

Soft X-ray tomography (SXT) is the only imaging technique that generates high-resolution, 3D views of cellular structures in large (up to 15 μm diameter), intact eukaryotic cells in the near-native state. Because SXT is conducted in the ‘water window’, the region of the spectrum where carbon and nitrogen absorb an order of magnitude more than water, it is particularly sensitive to the distribution of organic molecules in a cell. Absorption of photons at this wavelength adheres to Beer–Lambert’s law and is therefore linear with thickness (Attwood, 1999). Consequently SXT images are uniquely quantitative, and each organelle is seen based on its organic composition, which gives it an unique linear absorption coefficient (LAC) measure-

ment (Le Gros et al., 2005; Weiss et al., 2000). The difference in the LAC values of cellular components yields high-contrast images without the need for any chemical stains.

Cells imaged with SXT are typically between 1–15 μm in diameter, and each image shows all internal organelles superimposed in a 2D projection image. Tomographic reconstruction methods make it possible to retrieve that information and generate 3D views that reveal the spatial distribution of the organelles. It is well known that the optimal 3D reconstruction is achieved when images are taken at multiple intervals through 180°. With electron tomography, the combination of thin, planar specimens and the mechanical constraints of the specimen holders for these samples limits the ability to acquire images at all angles, and the quality of the reconstruction is compromised. Algorithms have been devised to minimize the artifacts in the reconstruction, but it is still not possible to obtain isotropic resolution. SXT can circumvent this problem by imaging cells in thin-walled (200 nm thin) capillary tubes. Images of cells in a capillary can be collected through an angular range of 180°, or even 360° to more evenly distribute the X-ray dose. As a consequence there is no wedge of missing information and, due to the incoherent bright field imaging geometry (Streibl, 1985), fully isotropic resolution can be achieved in the reconstructions. Full-rotation imaging has been used very successfully with SXT to generate 3D images of a wide variety of cell types with isotropic resolution (Carrascosa et al., 2009; Le Gros et al., 2005; McDermott et al., 2009; Meyer-Ilse et al., 2001; Schneider et al., 2010; Uchida et al., 2009, 2011).

The first step in processing data for high-resolution tomography involves the alignment of the projection images taken at different angles to a common axis of rotation. This is especially important for high-resolution techniques like electron tomography.
2. Results

Data processing programs operate on the assumption that the axis of rotation lies vertically. Since the long, thin custom-made glass capillary specimen holders used for SXT are not perfectly cylindrical, this is not always the case. Consequently there can be a small angle between the real axis of rotation (y) and the vertical axis of the CCD chip (Y), as diagrammed in Fig. 1. Additional imperfections in the rotation and translation stages cause additional movements of the specimen, which are not in accord with the model implicit in a standard tomographic reconstruction procedure. Fig. 2 shows the first and last images from an unaligned series of projection images collected through 180°. Strictly speaking the alignment correction can only be computed in a complete 3D space. However, given the geometry of our specimen holders, angular changes are relatively small, and good alignment and reconstruction results can be achieved by limiting alignment parameters to translations and one rotation in the plane of the projection images. With this approach we are taking into account differences between the angle of rotation and the vertical direction in the plane of imaging; components outside of this plane are ignored. As a result an independent tomographic reconstruction can be implemented in slices along the rotation axis (Castano-Diez et al., 2006; Fernandez, 2008; Mastronarde, 2008). Fig. 3 shows a comparison of digital orthoslices through a tomographic reconstruction of a yeast cell where the projections were aligned by translation cross-correlation and manual fiducial alignment. It is clear that the cross-correlation alignment is not sufficient in this case to give useful results. The main issue with this method by itself is that it is not robust and it produces inconsistent results frequently failing to produce a useable reconstructed SXT data set.

2.1. Alignment strategy

To discuss our alignment strategy, we first look at the geometric relationship between the 3D object to be reconstructed and its 2D projection images. During the image acquisition process, the sample is placed in a roughly cylindrical capillary tube that is rotated around an axis (y) through an angle, \( \omega_0 \). The axis of rotation may not be in the center of the cylindrical tube. Furthermore, the axis of rotation may not be parallel to the Y-axis (the vertical axis of the CCD camera, which is the vertical axis of the projection images), and the angle between the true axis of rotation (y) and the Y-axis may change as the tube is rotated due to stage imperfections. In addition to a tilt of the axis, stage drift may also produce horizontal and vertical shifts. The lack of a priori knowledge about the location of the rotation axis and the additional orientation changes due to the vibration of the stage makes the alignment and reconstruction problem a nontrivial task. The alignment strategy we developed aims to detect the inconsistency among different projection images and correct for the misalignment introduced by the systematic experimental errors.

If we assume the noise in the image is moderate, and can be described by a Gaussian distribution with zero mean, the alignment and reconstruction problem can be formulated as a nonlinear least squares problem of the form

\[
\min_{\{\psi_j, \phi_j\}} \sum_{j=1}^{m} \left| \left| P(\psi_j, \phi_j, s_j) f - b_j \right| \right|^2,
\]

where \( f \) is the 3D object to be reconstructed, \( (\psi_j, \phi_j) \) are two of the Euler angles that describe the orientation of the 3D object that yields the jth projection image \( b_j \). The projection image can be viewed simply as the a 2D image formed by applying a line integral operator \( P \) to the 3D object along a prescribed direction after the 3D
object has been rotated by \((\psi_j, \Phi_j)\), and translated by \(s_j\) (Yang et al., 2005). The azimuthal rotation angles are assumed to be known exactly, and for the single tilt-axis geometry the remaining Euler angles represent an in-plane rotation.

The optimization problem defined in (1) is generally difficult to solve due to the nonlinear coupling between the unknown 3D object and the orientation parameters \(\psi_j\) and \(\Phi_j\). One way to solve the problem, which is widely used in the cryoEM community, is to perform what is called a projection matching (Penczek et al., 1994). The projection matching algorithm can be viewed as a generalized coordinate descent algorithm. It requires an initial guess of the 3D object \(f\) (or the Euler angles \(\psi_j\) and \(\Phi_j\)) \(f_0\) and consists of the following two steps:

When \(f_0\) is available, an exhaustive search of the optimal orientation parameters \(\psi_j\) and \(\Phi_j\) is performed, i.e., we first solve

\[
\min_{\{\psi_j, \Phi_j\}} \sum_{j=1}^m ||P(\psi_j, \Phi_j, s_j)f_0 - b_j||^2 \tag{2}
\]

Once an optimal set of \(\psi_j\) and \(\Phi_j\) are determined, we can solve a linear least square problem by using a standard tomographic reconstruction algorithm, i.e., we solve

\[
\min_{f} \sum_{j=1}^m ||P(\psi_j, \Phi_j, s_j)f - b_j||^2 \tag{3}
\]

One of the key factors that affect the convergence of the projection matching algorithm is the availability of a good initial guess \(f_0\). For cryoEM image reconstruction, obtaining a good initial guess is generally a difficult task because the geometric relationship between the 3D object and 2D projection images is largely unknown a priori. However, for X-ray cell imaging, we have a better knowledge of the relationship between the projection image and the object even though we do not have the precise values of some of the orientation and translational parameters. In particular, the azimuthal rotation angles are known exactly, and in practice we have at least 91 images cover 180° viewing angles in 2-degree increments. In addition, the presence of the capillary tube edges in the projection images enables us to perform an initial alignment to fix the axis of rotation and obtain an initial estimate of the direction of the rotation axis relative to the \(y\)-axis.
To identify the angle between the actual rotation axis and the Y-axis, we first identify the tube edges associated with the 1st and the 91st images by using standard edge detection techniques. Without loss of generality, we can assume the azimuthal rotation angles associated with these two images are 0° and 180°. From the slope of these edges, we can calculate the angles between the tube edges and the Y-axis. If we denote the angle between the tube edges of the first image and the Y-axis by \( \beta_1 \), and that associated with the 91st image by \( \beta_2 \), and if we ignore additional rotation introduced by stage imperfections, then the angle \( \alpha \) between the rotation axis and the Y-axis should be \( \alpha = (\beta_1 + \beta_2)/2 \) (see Fig. 2).

By rotating each image by \( \alpha \), we effectively make the axis of rotation parallel to the Y-axis. However, the axis rotation does not necessarily pass the origin of the 3D coordinate space, nor does it have to be in the center of the tube. Although the quality of the 3D reconstruction does not depend on the exact location of the axis of rotation, computational efficiency can be gained if we choose the axis of rotation to go through the center of the tube. In this case, total size of the reconstruction volume is roughly the size of the cylindrical tube with little extra void space outside of the tube.

To correct for translational movement of the rotation axis resulting from the vibration of the stage, we perform a successive translational alignment between the ith and the \( i + 1 \)st images for \( i = 1, 2, \ldots, 90 \) using cross correlation. Such an alignment procedure eliminates most of the translational movement that depends on the azimuthal rotation angle \( \theta \). To account for a potentially global (angular independent) horizontal drift of each projection image by an unknown constant number of pixels \( A \), we flip the 91st image in the horizontal direction and cross correlate the flipped image with the first image. Because the x-coordinate of each pixel in the 1st and the 91st images can be represented by

\[
x = (x - x_0)\cos \theta + (y - y_0)\sin \theta + \Delta = x - x_0 + \Delta.
\]

and

\[
x'' = (x - x_0)\cos \pi + (y - y_0)\sin \pi + \Delta = -x + x_0 + \Delta.
\]

respectively, where \((x_0, y_0)\) is the unknown \((x, y)\) location of the rotation axis, the position of cross correlation peak yields \(2A\), which allows us to deduce the constant drift and shift each image by \(-A\) pixels to correct for such a drift. A similar correction can be made for a vertical drift also.

After the initial alignment steps described above have been performed, we crop each projection image to keep the projection of the sample and the capillary tube in the image. We then choose the axis of rotation to be in center of the cropped image and perform an initial 3D tomographic reconstruction. Because the axis of rotation is fixed, the 3D reconstruction can be reduced to \( n_z \) 2D reconstructions, where \( n_z \) is the number of \((x, z)\) slices in the y-direction. A number of algorithms can be used to perform the reconstruction task. We use the conjugate gradient (CG) algorithm because it produces a high quality reconstruction, is efficient and relatively easy to parallelize on a distributed-memory cluster. Typically, 15 or fewer CG iterations are sufficient to produce a 3D reconstruction with desired resolution. Running too many CG iterations may amplify undesirable noise in the data. The iteration number can be viewed as a regularization parameter for the CG based iterative reconstruction algorithm (Hansen, 1998).

The additional azimuthal angular dependent in-plane rotations of the projection images introduced by imperfections in the stage are corrected in a simplified projection matching procedure that follows the initial alignment. In this simplified projection, we generate a set of reference projections from a 3D model constructed in the previous iteration computationally. Both translation and rotational cross-correlations are performed between each reference projection image and the corresponding experimental image (after it is properly cropped). The translational shifts and in-plane rotation angles are used to transform each experimental image before the transformed images are cropped and used to produce a new 3D reconstruction. This procedure is repeated until the changes in shifts and angles fall below a chosen threshold. The flowchart in Fig. 4 gives a summary of our alignment procedure.

In implementing the code, we focused on MPI (message passing interface) parallelization for distributed memory clusters that have a limited amount of local memory (Pacheco, 2011). Although our parallelization tends to significantly reduce the required time for the reconstruction and alignment process, our main focus in the distributed-memory parallel implementation is to address the memory-limitation problem. The alignment and reconstruction procedure described above requires two different types of data distribution schemes that are currently coordinated through disk I/O. For the initial alignment, it is natural to distribute experimental images among different processing units. Each processing unit contains a fixed number of images. Successive translational alignment is performed simultaneously on local images assigned to individual processors. The aligned images are written to the disk as a single rotation, the position of cross correlation peak yields 262 Y. Parkinson et al. / Journal of Structural Biology 177 (2012) 259–266
image stack, which requires synchronization. When the image stack containing the aligned images is read into the memory again for reconstruction, each image is partitioned evenly along the y direction, and each processing unit receives $m$ sub-images that it can use to reconstruction a portion of the 3D object.

In the simplified projection matching procedure, reference sub-images are generated from a partial 3D volume produced from the previous iteration, the reference sub-images are merged when they are written to the disk as a single file. The merged reference images are read back from the disk and redistributed among different processors on an image-by-image basis so that the cross-correlation between the reference projection and experimental images can be performed in parallel.

To characterize the performance of AREC3D, we measured wall clock time while running it with different numbers of processors for a data set with 91 projections that was originally 1024 × 1024 pixels, then cropped to 500 × 800 pixels. For 1, 2, 4, 8, 16, 32, 64, and 128 processors, the time to complete one iteration was 1600, 800, 410, 225, 120, 72, 56, and 35 seconds. As the number of processors increases, it becomes difficult to divide 91 images evenly among processors. In addition, I/O overhead means that the scaling is not perfectly linear.

Although our current parallelization scheme incurs some I/O overhead, the overhead is moderate. Even though the total amount of memory for the latest machines tends to increase, memory per processing unit remains the same, and is projected to decrease in the future. Therefore, we decided to perform I/O in this version of the code to make it more flexible. We are also developing a shared-memory parallel version of the code that can be used on a multi- and many-core mode with a large amount of shared memory using OpenMP. The OpenMP version does not use any I/O other than reading the 2D images and writing out the reconstructed 3D reconstruction. This version will be modified to run on a GPU using CUDA. In addition, we plan to develop a hybrid MPI and OpenMP parallel version of the code that can be used on multi- and many-core clusters (Agullero and Fernandez, 2011; Castano-Díez et al., 2008a; Xu et al., 2010).

2.2. Testing and validation

In this section we present results on the testing and validation of our method using two data sets: an artificially generated phantom, and a representative SXT data set. The test phantom was generated using a combination of Matlab scripts and functions from a freely available image reconstruction toolbox (Fessler, 1995, 2009). The 3D phantom is modeled as a water-filled glass tube in which there is an ellipsoidal cell that contains one high-contrast and one low-contrast internal organelle. Nanoparticles attached to the outside wall of the tube were built into the model for use in manual alignment procedures. The soft X-ray absorption characteristics of the objects in the phantom were chosen to match those obtained from SXT measurements of real cells. The axis of the capillary tube wall, which is circular; a poor alignment makes the tube non-circular, and in some cases completely discontinuous (compare to the results shown in Fig. 3). The manual and AREC3D aligned data sets as shown in Fig. 5 yield nearly identical results, and in both cases yield a nearly circular tube. A comparison of features in identical reconstructed slices obtained by each method through the volume is difficult because, as will be discussed below, the biggest difference between the manual and automatic alignment is the in-plane rotation correction of the images. This means that a reconstruction based on AREC3D is at a slightly different orientation to that obtained from manual alignment. Visual inspection indicates that the reconstruction quality, although very similar, is marginally better for the manual alignment.

To quantify the difference between the alignment correction obtained using manual fiducial marker location and AREC3D, we have plotted the x and y position and in-plane rotation alignment corrections as a function of projection angle for both manual and AREC3D alignment of the SXT data set (Fig. 6). The two methods

![Image](337x81 to 537x364)

**Fig. 5.** Orthoslices through the reconstructions of both the phantom (A) and the soft X-ray tomography data (B), using both automatic alignment (top) and manual alignment method (bottom). Slices were taken at different positions along the tube axis. Scale bar = 1 μm.
give an equivalent alignment correction for the phantom data set with 100 iterations used for the AREC3D alignment (data not shown). Fig. 6 also shows the difference between the x translations for manual vs. AREC3D alignment, and we find that the difference follows a sine curve; simply stated these two x alignments yield essentially identical volumes that are slightly shifted from each other. We found that this agreement between manual and AREC3D alignment holds for essentially all data sets tested. We believe this occurs because we use a cylindrical specimen geometry with a lateral extent less than the field of view of the microscope; and most data sets contain projection images with high-contrast edge features, making the in-plane translational alignment of the data set in a direction normal to this edge very straightforward.

The differences between manual and AREC3D alignment for y position and in-plane rotation corrections are more significant. Although the difference curve follows a sine curve, greater fluctuation is observed. This indicates that an accurate alignment in the y-direction is more difficult to achieve in the absence of image features that have a strong contrast jump in the y direction. The rotation parameter is much smoother in the manual alignment due to a grouping parameter available in the IMOD software (Kremer et al., 1996). This parameter forces a smooth transition of the rotation parameter between projections. We empirically found that using this grouping parameter produces better reconstructions. A similar smoothing function will be implemented in future versions of the AREC3D software. In Fig. 7 we demonstrate improvements in the reconstruction quality based on the number of iterations used for projection matching. Distortions can be seen clearly in the cell walls at the top of the two cells. These discontinuities vanish nearly completely with increased iteration number. Subcellular organelles, such as the nucleus, nucleolus, vacuoles and lipid bodies, can be clearly seen in both automatic and manual alignment.

Finally we compare reconstruction quality in manual alignment and AREC3D alignment using a noise compensated leave one out method. In this method, reconstructions are calculated based on a projection stack with one projection angle missing. An approximation to the deleted projection is generated from the reconstructed volume and compared to the original, omitted projection using standard FRC methods (Saxton and Baumeister, 1996).
This process is repeated every 10 images and the results are averaged, as shown in Fig. 8. For the microscope settings used for data collection in this work (32 nm pixel size), and with a FRC threshold of 0.5, the resolution obtained for the different reconstruction methods is 87 nm for the manually aligned data and 94 nm for the AREC3D aligned data. Despite some differences in the y-shifts and in-plane rotations, the overall quality of the reconstruction obtained using AREC3D is satisfactory for data analysis (e.g. segmentation). For analyses requiring the best resolution or optimized contrast the AREC3D derived alignment parameters can be used as the initial input to a more thorough analysis procedure. For instance, with human intervention “bad” projections caused by an uncontrolled seismic noise could be removed from the data prior to alignment, leading to improvement over automatic procedures.

3. Discussion

Development and implementation of the AREC3D software package are significant steps forward for high throughput soft X-ray tomography. Tight integration of automatic alignment and tomographic reconstruction has enabled investigators using SXT at the NCXT to obtain almost real-time feedback on the data as it is being collected using only a few iterations of projection matching in AREC3D. An increased number of iterations can be used for later refinement. The prompt reconstructions obtained using AREC3D are invaluable to investigators performing SXT experiments; by using binned images rather than full-resolution images, reconstructions could be obtained even more quickly. The ability to obtain high-resolution cellular tomograms while examining a large

Fig. 7. Orthoslices along the rotation axis through the reconstruction using different numbers of iterations of projection matching. Number of iterations, top: 2, 5, 10, 25 (left to right); bottom 50, 75, 100 (left to right) and manual alignment (bottom, far right). Scale bar = 1 μm.

Fig. 8. Comparison of Fourier Ring Correlation (FRC) curves calculated with the leave-on-out method (data has 32 nm pixel size). The dotted line indicates the 0.5 threshold. Manual alignment shows slightly better results than AREC3D automatic alignment with 100 iterations.
number of cells under different conditions enables intelligent decision making during the experiment.

In many cases, the volumes obtained after convergence of the algorithm are sufficient for further processing; in some cases, they are of sufficient quality to allow selection of a few data sets that can be reconstructed using fiducial markers to get improved resolution. SXT image processing will continue to leverage off state-of-the-art developments in electron tomography, but the unique ability to examine large numbers of cells, and the enormously relaxed demands on specimen geometry, makes it necessary to implement new software optimized for SXT.

AREC3D is a small but significant component of an automated data analysis pipeline for high-throughput SXT. As the number of biological soft X-ray microscopy facilities increases (Pereiro et al., 2009), there will be many additional creative contributions to the portfolio of software tailored to SXT. New software is required for virtually every aspect of the SXT data processing pipeline, from the difficult problem of automatic segmentation to data knowledge bases (DOE, 2010) for archiving and mining the unique data obtained with SXT and with correlated high N.A cryo-luminescence microscopy (McDermott et al., 2009).

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